

# 1-4 Screw Shaft Design

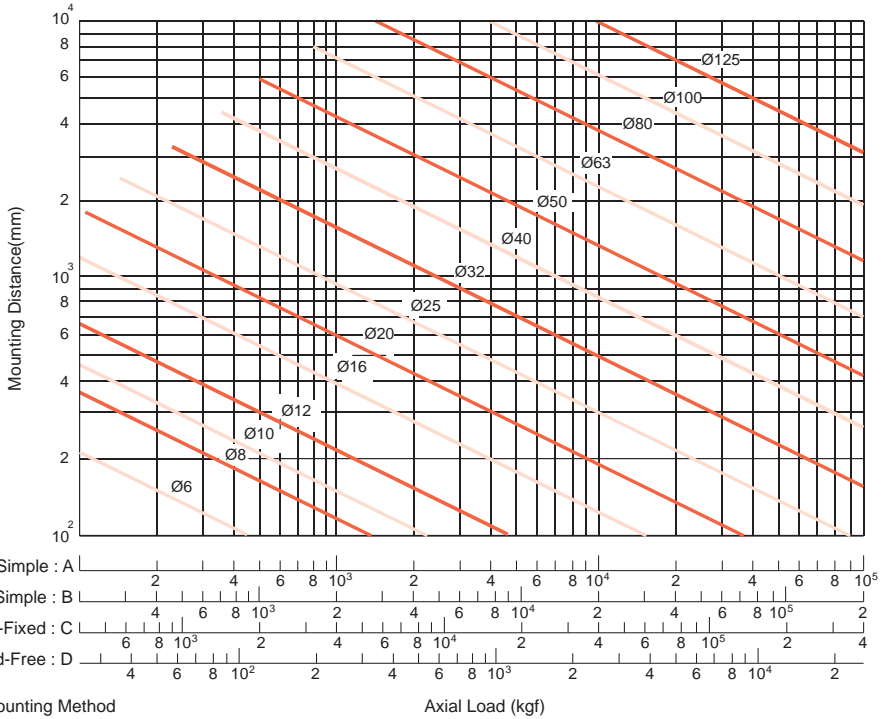


Fig 1.4.16 Buckling Load vs. Nominal Diameter and Length

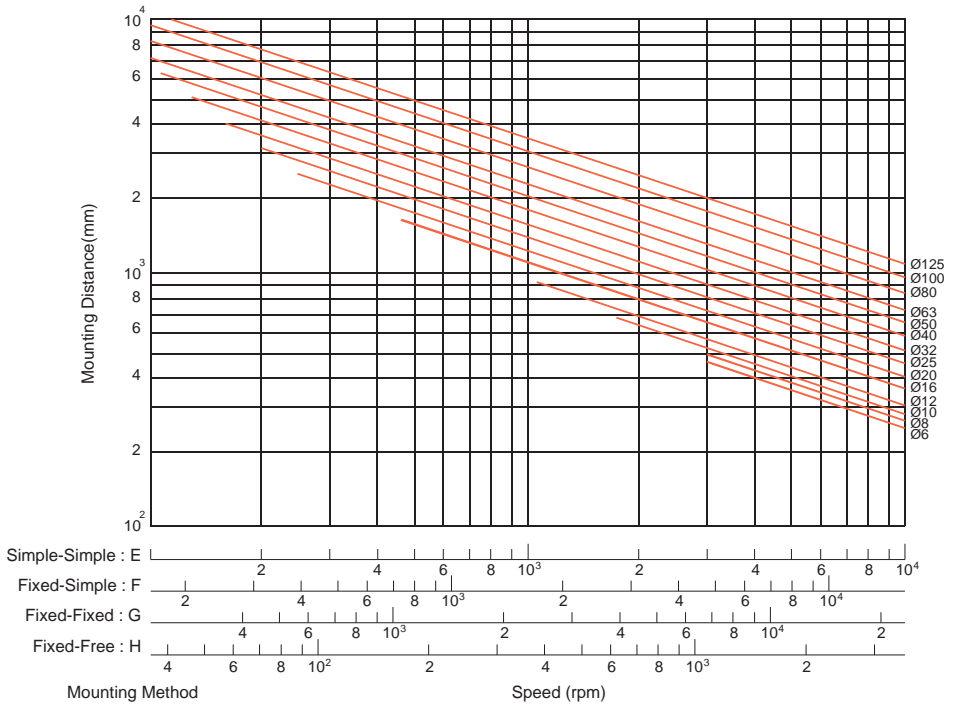


Fig 1.4.17 Buckling Load vs. Nominal Diameter and Length

## 1-4 Screw Shaft Design

### ■ 1-4-3 Critical Speed

#### (1) Dangerous speed

To prevent the screw's natural frequency attain resonance which will occur critical speed, it's necessary to look into the ball screw allowable rotation speed ( Below 80% of the Critical Speed ). More detail of allowable rotation speed classified though screw diameter please refer to Fig 1.4.17.

#### (2) $dm \cdot n$ value

The allowable rotation speed is regulated also by the  $Dm \times N$  value ( $Dm$  : diameter of central circle of steel ball,  $N$  : Revolution speed, rpm) which expresses the peripheral speed.

Generally,

For precision

(accuracy grade C7 to C0)  
 $Dm \times N \leq 70,000$

For general industry (C10)  
 $Dm \times N \leq 50,000$

If your requirement about the product will exceed the limitation, please contact with TBIMOTION to discuss the detailed solution for the ideal product.

※ When  $\epsilon$ , the ratio of screw length and shaft diameter has exceeded 70, please contact with TBIMOTION to arrange the special arrangement for production.

$$n = \alpha \cdot \frac{60\lambda^2}{2\pi L^2} \sqrt{\frac{Eg}{\gamma A}} = f \frac{dr}{L^2} \cdot 10^7 (\text{rpm})$$

Where

$\alpha$  : Safty factor ( $\alpha = 0.8$ )

$E$  : Verticle elastic modules ( $E = 2.1 \cdot 10^4 \text{kgf/mm}^2$ )

$I$  : Minimum secondary torque of axial section plane

$$I = \frac{\pi}{64} dr^4 (\text{mm}^4)$$

$dr$  : Screw shaft root diameter (mm)

$g$  : Acceleration of gravity ( $g = 9.8 \cdot 10^3 \text{mm/s}^2$ )

$\gamma$  : Density ( $\gamma = 7.8 \cdot 10^{-8} \text{kgf/mm}^3$ )

$A$  : Screw shaft sectional area ( $A = \pi dr^2/4 \text{mm}^2$ )

$L$  : Mounting distance (mm)

$f, \lambda$  : Coefficient determined from the ball screw mounting method

Floated-Floated  $f = 9.7$  ( $\lambda = \pi$ )

Fixed-Floated  $f = 15.1$  ( $\lambda = 3.927$ )

Fixed-Fixed  $f = 21.9$  ( $\lambda = 4.730$ )

Fixed-Free  $f = 3.4$  ( $\lambda = 1.875$ )

## 1-5 Driving Torque

### ■ 1-5-1 Driving torque $T_s$ of the transmission shaft

$T_s = T_P + T_D + T_F$  (in fixed speed)

$T_s = T_G + T_P + T_D + T_F$  (when accelerating)

$T_G$  : Acceleration torque (1)     $T_P$  : Load torque (2)

$T_D$  : Preload torque (3)         $T_F$  : Friction torque (4)

#### (1) Acceleration $T_G$

$$T_G = J\alpha \text{ (kgf} \cdot \text{cm)}$$

$$\alpha = \frac{2\pi n}{60\Delta t} \text{ (rad/s}^2\text{)}$$

$J$  : Moment of inertia (kgf · cm · s<sup>2</sup>)

$\alpha$  : Angular acceleration (rad/s<sup>2</sup>)

$n$  : Revolutions (min<sup>-1</sup>)

$\Delta t$  : Starting time (sec)

#### (3) Preload torque $T_D$

$$T_D = \frac{K \cdot P_{PL} \cdot \ell}{\sqrt{\tan \alpha} \cdot 2\pi} \text{ (kgf} \cdot \text{cm)}$$

$K$  : Internal coefficient

(0.05 is usually adopted)

$P_{PL}$  : Preload (kgf)

$\ell$  : Lead (cm)

$\alpha$  : Lead angle

#### (4) Friction torque $T_F$

$$T_F = T_B + T_O + T_I \text{ (kgf} \cdot \text{cm)}$$

$T_B$  : Friction torque of bracing shaft

$T_O$  : Friction torque of free shaft

$T_I$  : Friction torque motor shaft

#### (2) Lead torque $T_P$

$$T_P = \frac{P \cdot \ell}{2\pi\eta_1} \text{ (kgf} \cdot \text{cm)}$$

$$P = F + \mu Mg$$

$P$  : Axial load (kgf)

$\ell$  : Load (cm)

$\eta_1$  : Positive efficiency

The efficiency when rotating motion is altered to linear motion

$F$  : Cutting force (kgf)

$\mu$  : Friction

$M$  : Mass of moving object (kg)

$g$  : Acceleration of gravity (9.8 m/s<sup>2</sup>)

$$T_P = \frac{P \cdot \ell \cdot \eta_2}{2\pi} \text{ (kgf} \cdot \text{cm)}$$

$\eta_2$  : Reverse efficiency

The efficiency when linear motion returns to rotating motion

The friction torque of the bracing shaft would be affected by the volume of lubrication oil. Besides, be careful with the excessive tight end seal may lead to unexpected over friction torque or temperature rise.

【For reference】 Moment of inertia of load (refer to Table 1.5.1)

$$J = J_{BS} + J_{CU} + J_W + J_M$$

$J_{BS}$  : Moment of inertia Ball screws shaft

$J_{CU}$  : Moment of inertia Coupler

$J_W$  : Moment of inertia Linear motion part

$J_M$  : Moment of inertia Roller shaft part of motor shaft

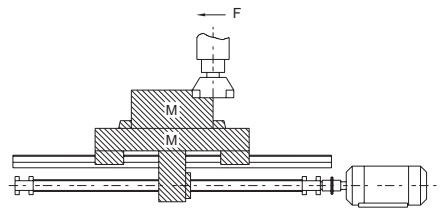


Fig 1.5.1 Moment of inertia of load

## 1-5 Driving Torque

Table1.5.1 Conversion formula for moment of inertia of load

Formula	J
Moment of inertia converted from motor shaft	
Cylinder load	$\frac{\pi \rho L D^4}{32}$
Linearly moving object	$\frac{M}{4} \left( \frac{V \ell}{\pi \cdot N_M} \right)^2 = \frac{M}{4} \left( \frac{P}{\pi} \right)^2$
Unit	kg . m <sup>2</sup>
Moment of inertia during deceleration	$J_M = \left( \frac{J_\ell}{N_M} \right)^2 J \ell$

$\rho$  : Density (kg/m<sup>3</sup>)  $\rho = 7.8 \cdot 10^3$

L : Cylinder length (m)

D : Cylinder diameter(m)

M : Mass of the linear motion part (kg)

V : Velocity of the linear moving object (m/min)

N<sub>M</sub> : Motor shaft revolutions (min<sup>-1</sup>)

P : The moving magnitude of the linearly moving object per rotation of the motor (m)

N $\ell$  : Rotations in longitudinal moving direction (min<sup>-1</sup>)

J $\ell$  : Moment of inertia in load direction

J<sub>M</sub> : Moment of inertia in motor direction

### ■ 1-6-1 Selection of Nut

#### (1) Series

When making selection of series, please take demanded accuracy, intended delivery time, dimensions( the outside diameter of screw, ratio of lead/ the outside diameter of screw) preload and etc into consideration.

#### (2) Circulation type

Selection of circulation type : Please consider the efficiency of screw nut's mounting space. The advantage of each circulation type will be specified in figure 1.6.1.

#### (3) Number of loop circuits

Performance and service life should be considered when selecting number of loop circuits.

#### (4) Shape of flanges (FLANGE)

Please make selection based on the available space for the installation of nuts.

#### (5) Oil hole

Oil holes are provided for the precision ball screws, please use them during machine assembling and regular furnishing.